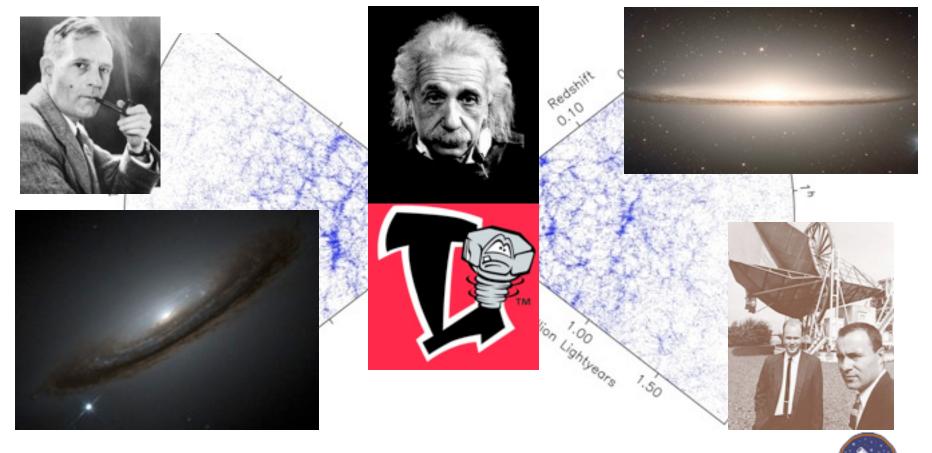
Introduction to Cosmology: Lifestyles in an Expanding Universe





Brian Fields University of Illinois

TALENT Summer School in Nuclear Astrophysics

MSU/NSCL | June 2, 2014

Syllabus: Part I

★ Cosmology Primer

- evidence for an expanding universe
- life in an expanding universe
 - dynamics of an expanding universe

The Cosmic Microwave Background (CMB)

★ Cosmic Acceleration



- Structure, Origin, Evolution of the Universe today: stars organized into galaxies today: stars organized into galaxies today: stars organized into galaxies
- Typical galaxy: 100 billion stars

Andromeda galaxy





Sombrero galaxy

- Structure, Origin, Evolution of the Universe
 ★ today: stars organized into galaxies
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Think big! galaxies are building blocks

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Hubble Ultra Deep Field





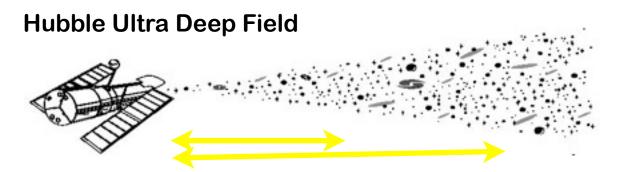




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far away = long ago telescopes are time machines!

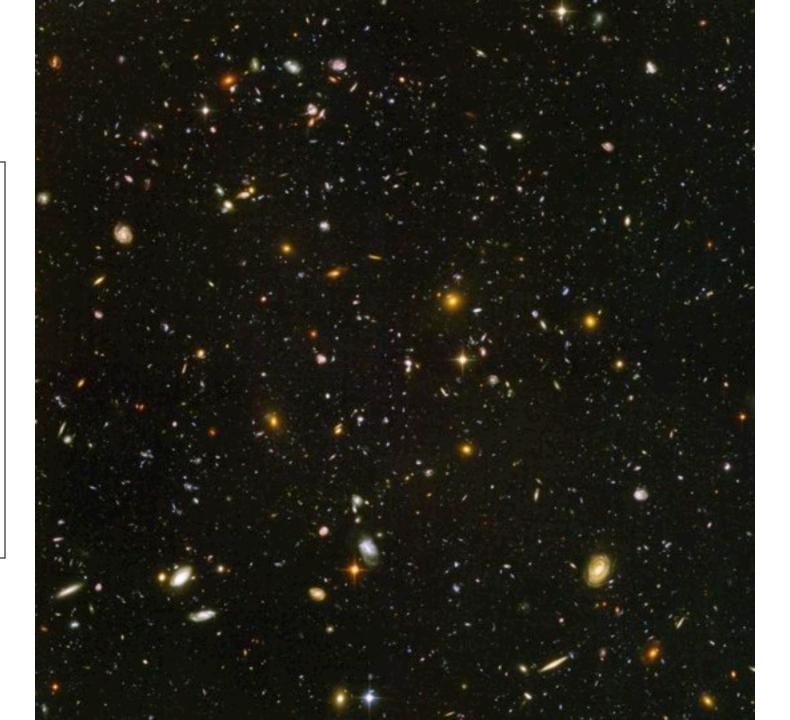
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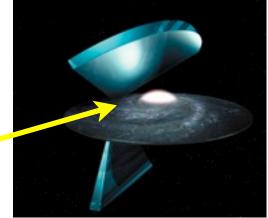
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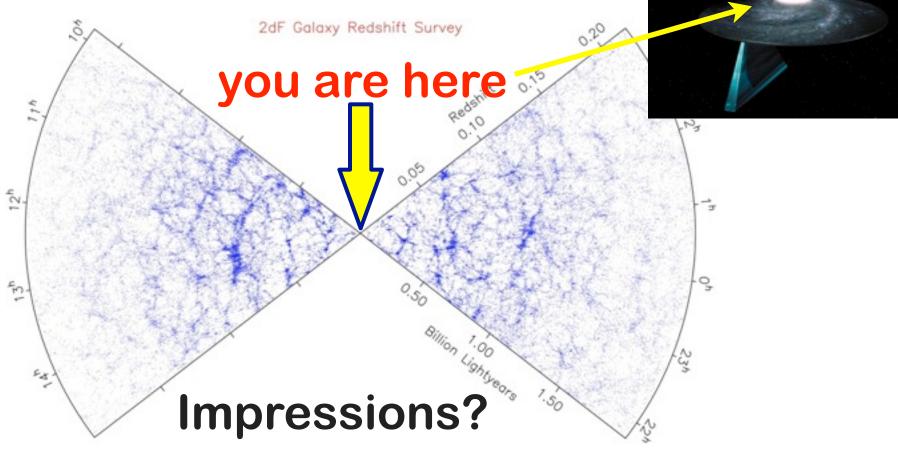
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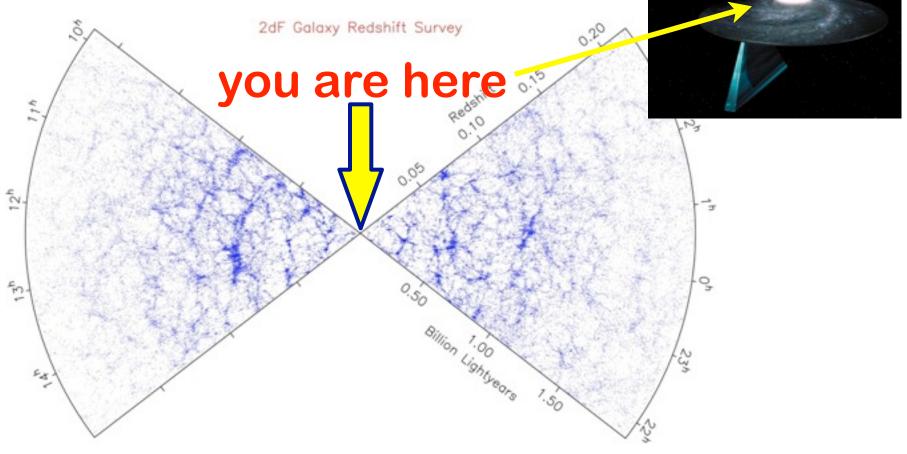


you are here

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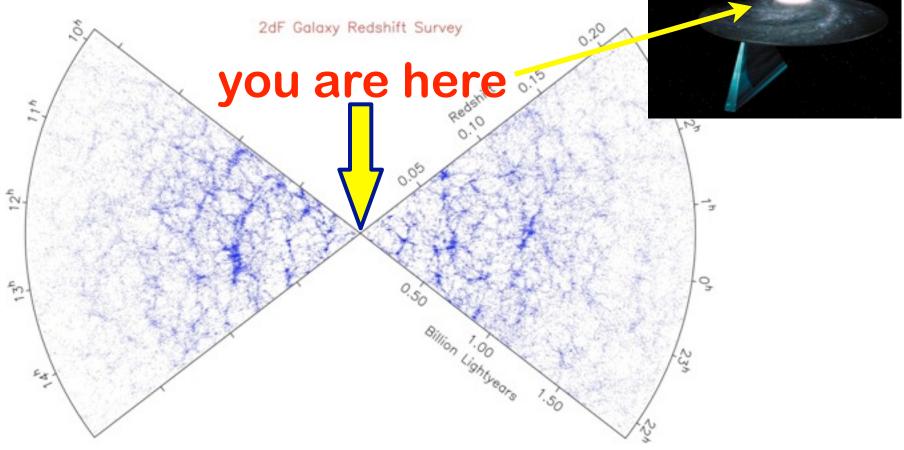


Measure cosmic structure: map galaxies in space



On small scales: galaxies clumpy

Measure cosmic structure: map galaxies in space



On large scales: galaxies smoothly fill universe: homogeneous + isotropic = "Cosmological Principle"

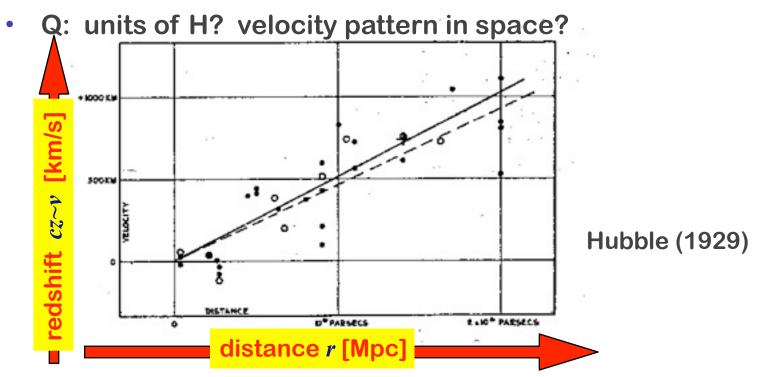
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- all galaxies redshifted: move away from us
- farther faster:
- that is,
- Q: units of H? velocity pattern in space?



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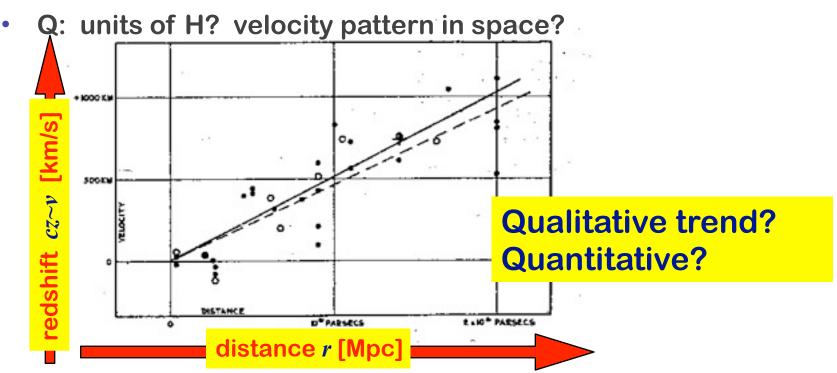
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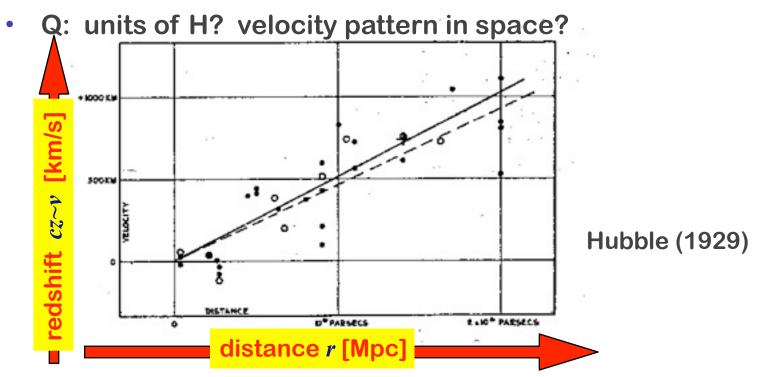
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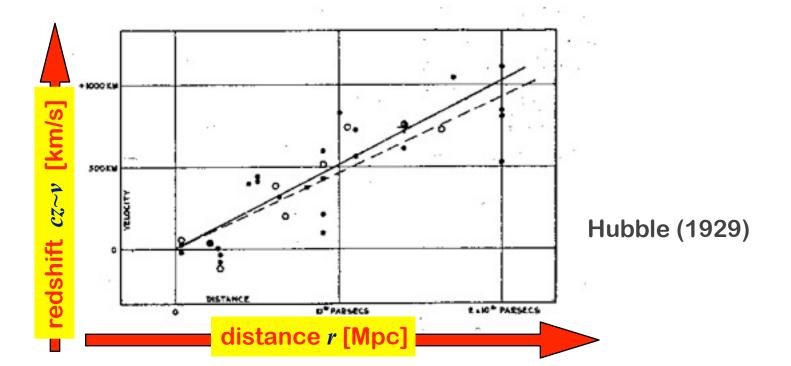




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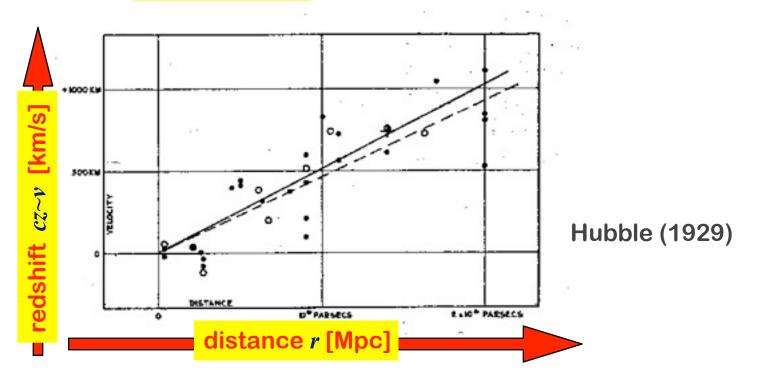




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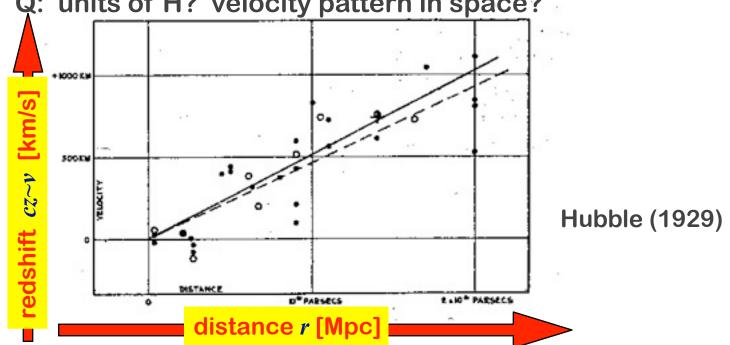


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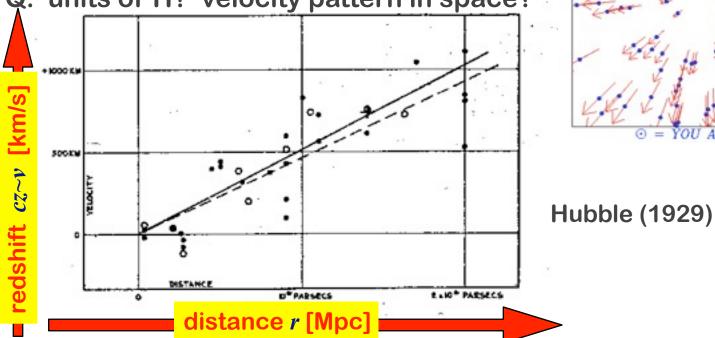
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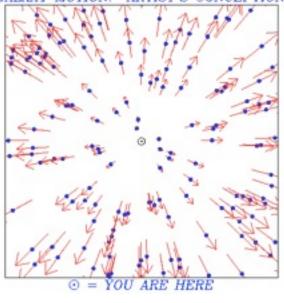


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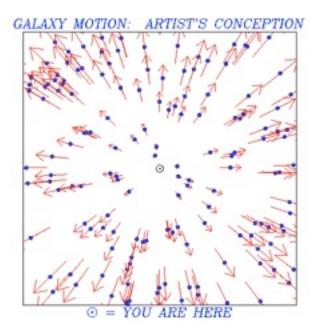






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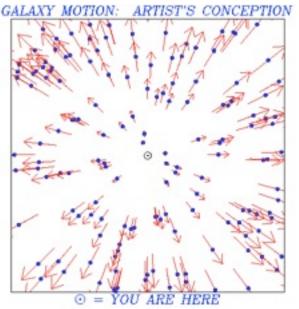
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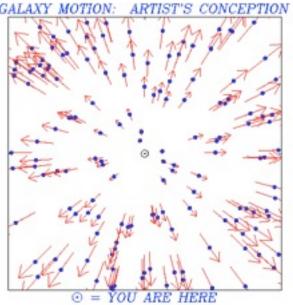


Interpretation: What does it mean?

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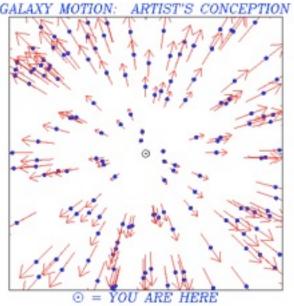
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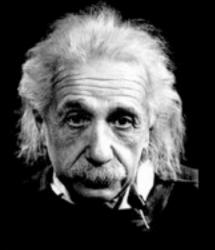
Egoist view:

We are at center of Universe



≻Einstein view

Universe is expanding! No center!



Explaining Hubble: Kinematic Model of Milne (1933)

imagine an explosion at t = 0

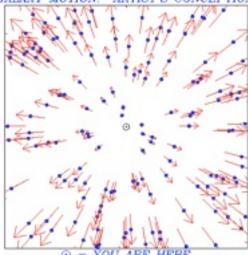
- let galaxies all start in region of size $\ll ct_{today}$ fly away with uniform distribution speeds v_{gal}
- but we remain at r = 0 until now: $t_{today} = t_0$

after explosion, let each galaxy *coast* maintaining its initial velocity

after time $\Delta t = t_0$:

- $\vec{r}_{gal} \rightarrow \vec{v}_{gal} \ t_0$ fastest \rightarrow farthest!
- so $\vec{v}_{gal} \rightarrow \vec{r}_{gal}/t_0 \equiv H_0 \vec{r}_{gal} \propto \vec{r}_{gal}$: recover Hubble's law!
- solve for cosmic age

$$t_{0,\text{Milne}} = \frac{1}{H_0}$$



Hubble Flow: Characteristic Scales

Hubble's law today: $\vec{v} = H_0 \vec{r}$ introduces Hubble parameter $H_0 = 100 \ h \ \rm km \ s^{-1} \ \rm Mpc^{-1}$ with $h \approx 0.7$

Hubble time

$$t_{\rm H} \equiv \frac{1}{H_0} = 9.778 \ h^{-1} \ {\rm Gyr} = 13.97 \ {\rm Gyr} \left(\frac{0.70}{h}\right)$$

where 1 Gyr = 10^9 years \Rightarrow sets \sim scale of "expansion age" of Universe

Hubble length

$$d_{\rm H} \equiv \frac{c}{H_0} = ct_{\rm H} = 2.998 \ h^{-1} \ {\rm Gpc} = 4.283 \ {\rm Gpc}\left(\frac{0.70}{h}\right)$$

sets \sim size of *observable* Universe

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But...

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Q: give an observational reason why we don't believe this?

Critiques of Cosmic Egoism

We are at the center of the universe?

Philosophically:

not Copernican ("principle of mediocrity")

Physically:

haven't included gravity!

Observationally:

- Milky Way, Local Group don't look special
- not what expect from center of explosion
- compare supernova \rightarrow neutron star, black hole
- ...yet radial v pattern makes us look special...

Explaining Hubble: Einstein & General Relativity

Einstein (1915): General Relativity:

• spacetime warped by matter: "stretches like rubber sheet"



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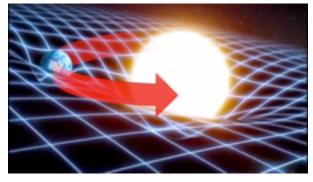


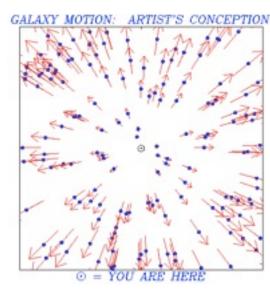
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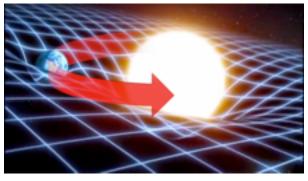
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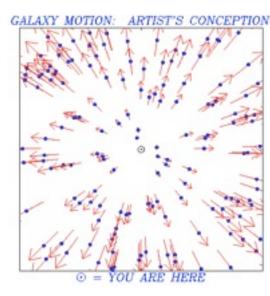
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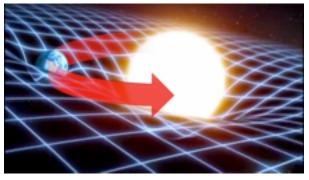


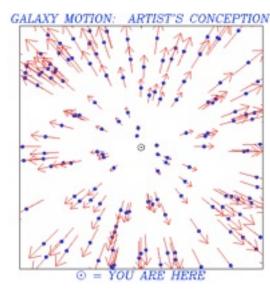
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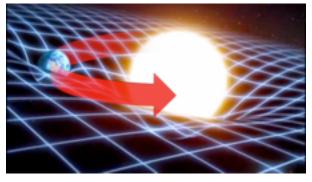


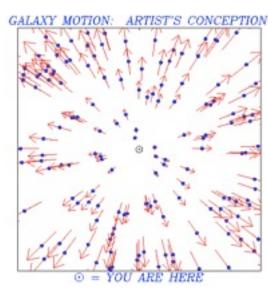
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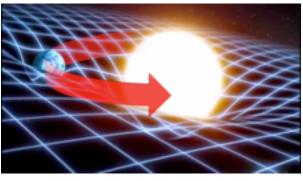


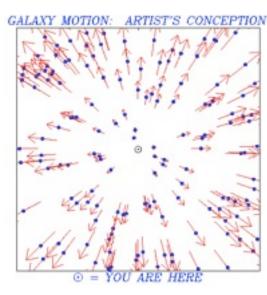
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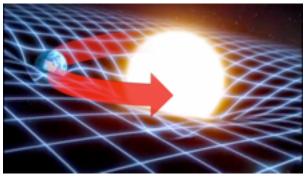


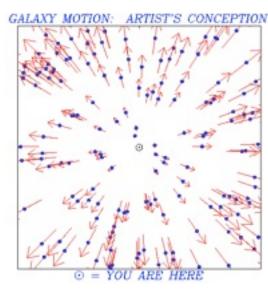
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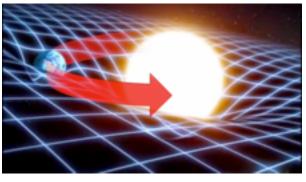


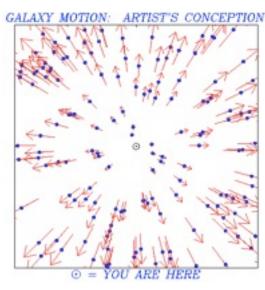


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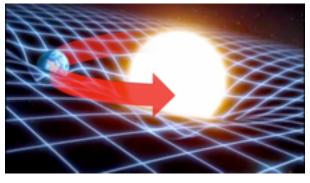


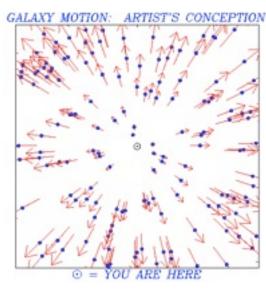


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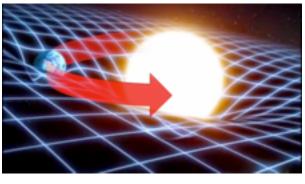
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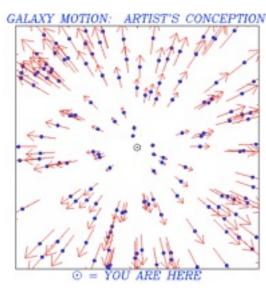
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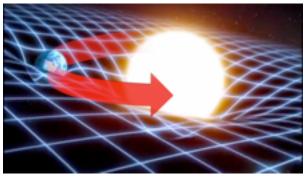
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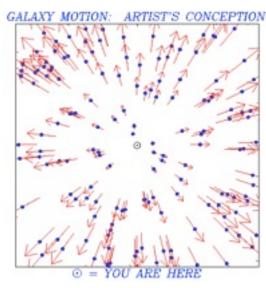
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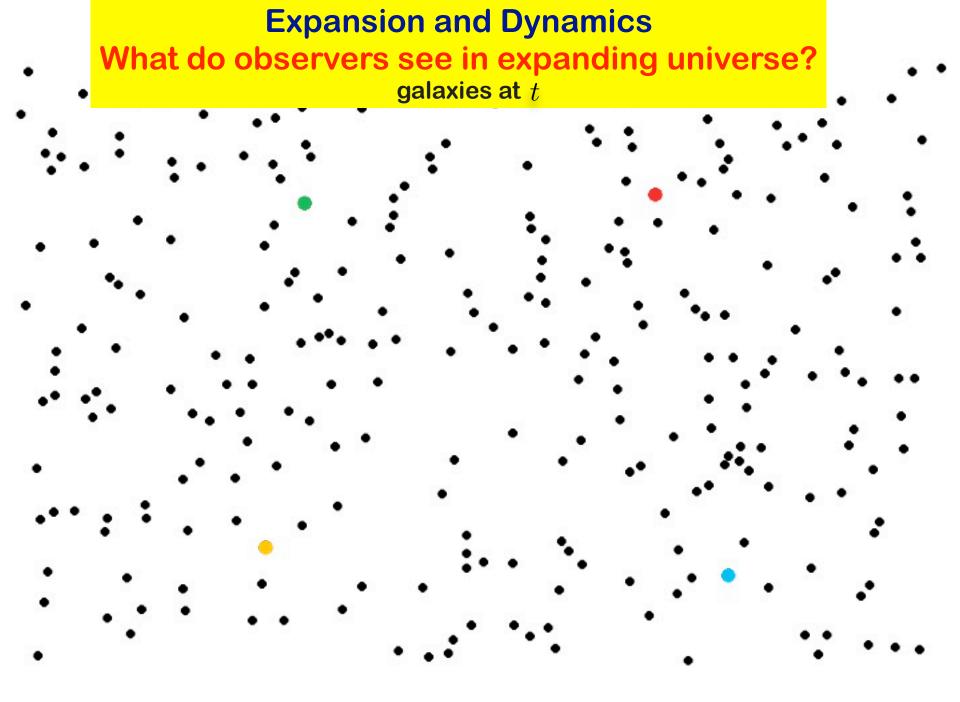
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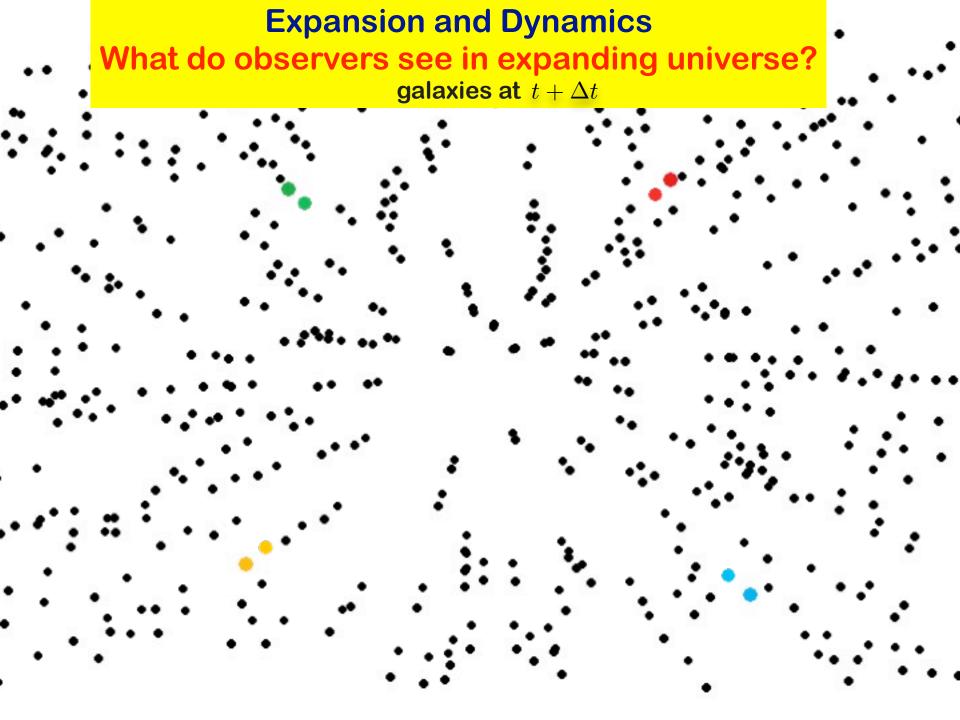
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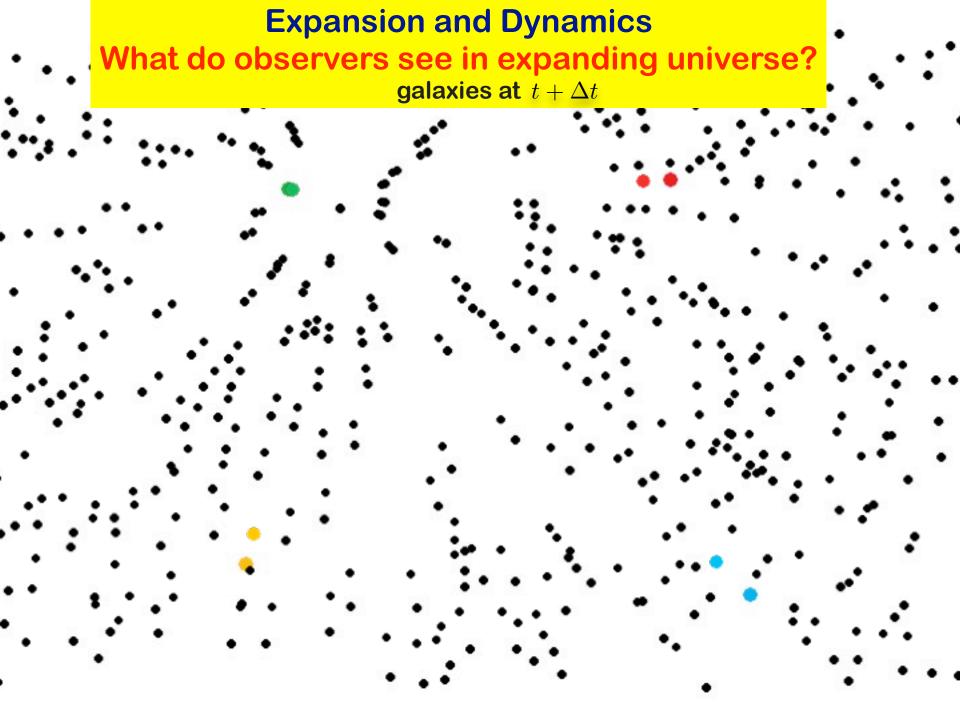
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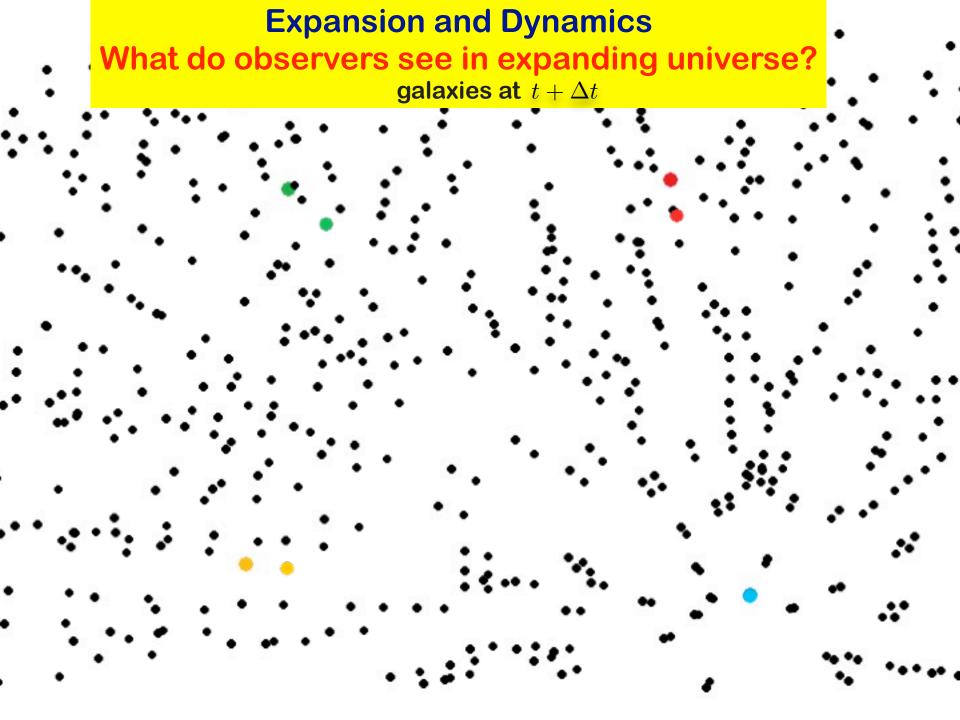


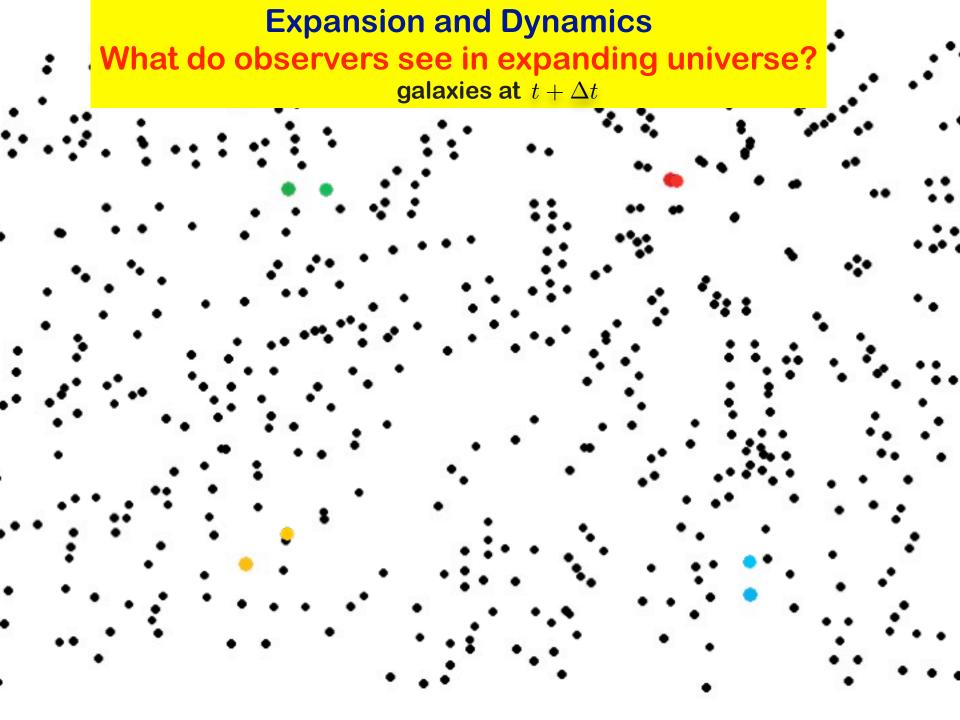


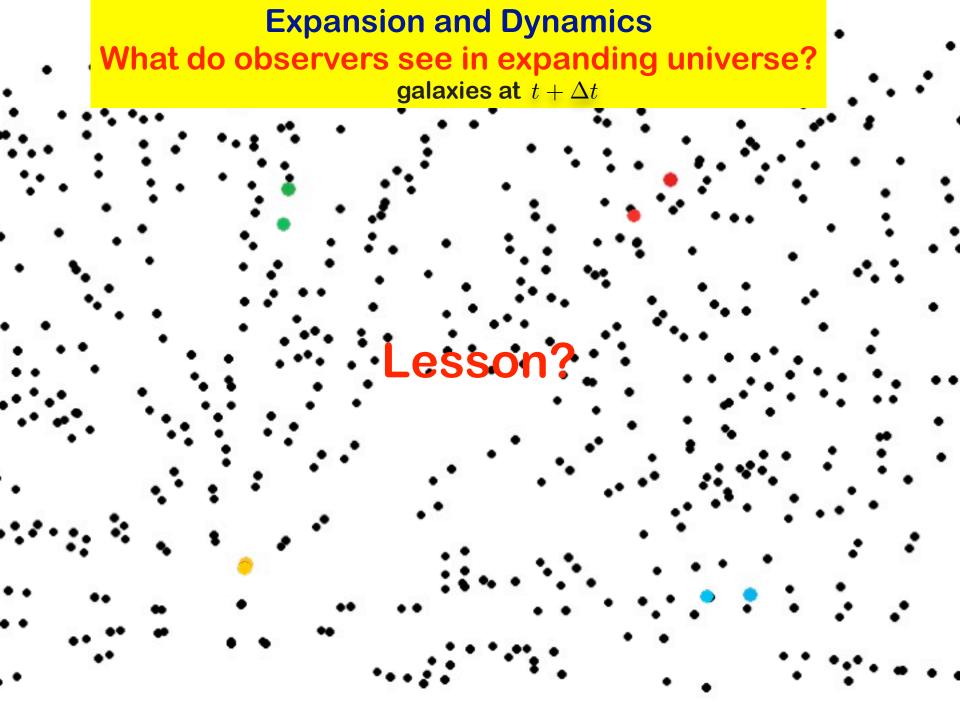


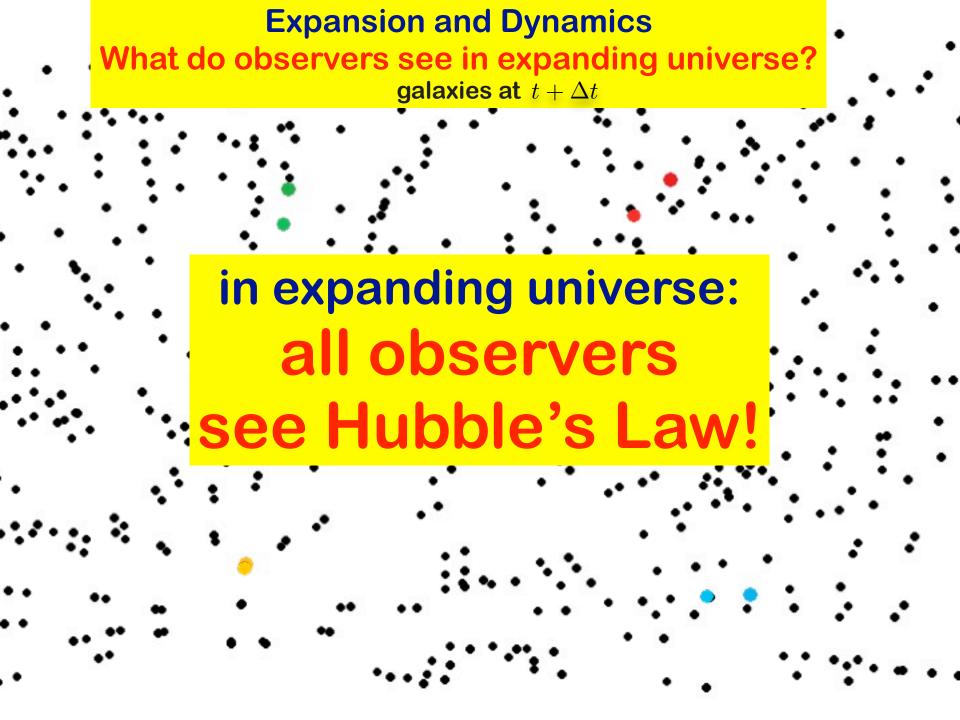












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expansion speed:

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$$H(t) = \frac{a}{a}$$

cosmic expansion rate

Expansion and Redshifts: I

quick-n-dirty: wavelengths are lengths! ...it's right there in the name! \rightarrow expansion stretches photon λ

 $\lambda ~\propto~ a$

if *emit* photon at t_{em} , then at later times

$$\lambda(t) = \lambda_{\text{emit}} \frac{a(t)}{a(t_{\text{em}})}$$

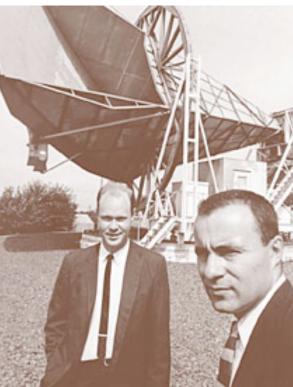
if observe later, $\lambda_{obs} = \lambda_{em} a_{obs}/a_{em}$ measure redshift today:

$$z = \frac{\lambda_{obs} - \lambda_{em}}{\lambda_{em}} = \frac{1 - a_{em}}{a_{em}}$$

high $z \leftrightarrow$ small $a \leftrightarrow$ distant past

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"...within the limits of our observations, isotropic, unpolarized, and free from seasonal variations"



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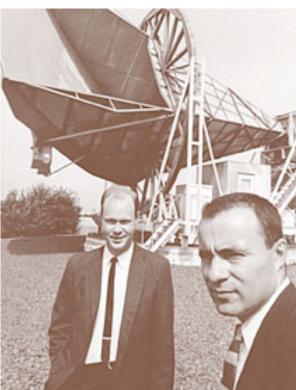


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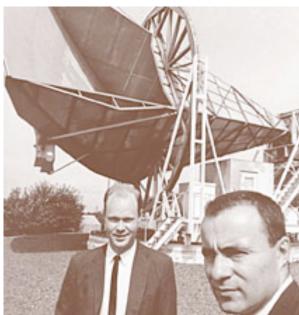
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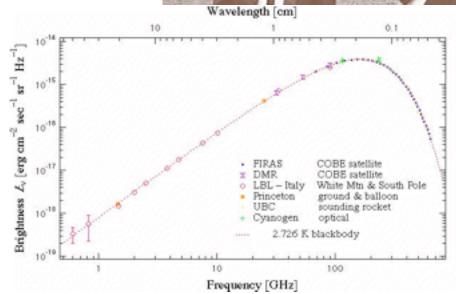
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spectrum: Planck form





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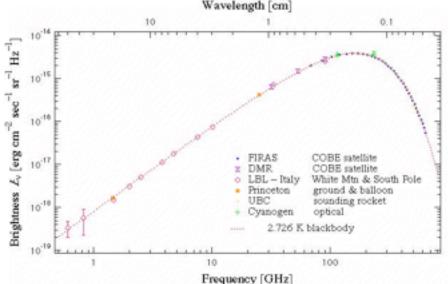
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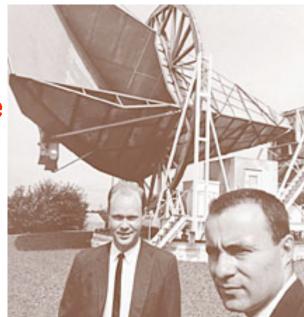
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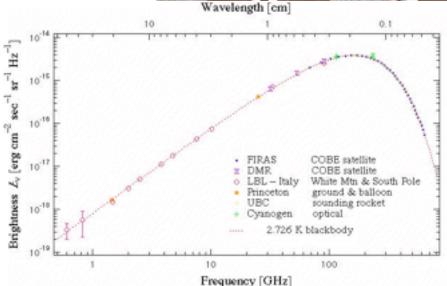
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- consider arbitrary point, in homogeneous U of density
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- Homework: show that Newtonian gravity gives

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Lessons:

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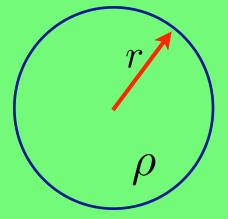
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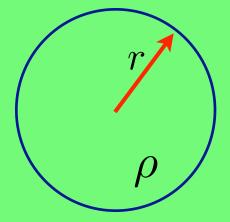
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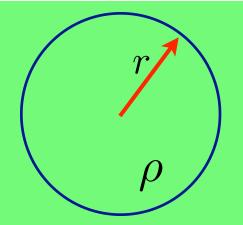
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spoiler alert: curvature term is zero

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- Q: so if we measure expansion history H(z)...?
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- quick and dirty: Hubble law
- lesson: need redshift z (trivial!) and distance r (non-trivial!)

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• object with known, fixed luminosity L = light power output

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Q: requirements for a useful standard candle? Candidate(s)?



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 must understand emitter well
 preferably candles identical at all cosmic time
 or must understand how they evolve
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Best candidates: well-calibrated, huge L

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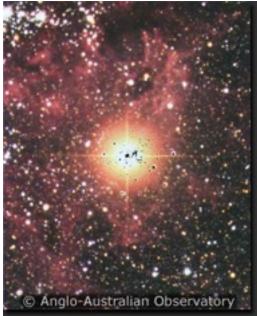


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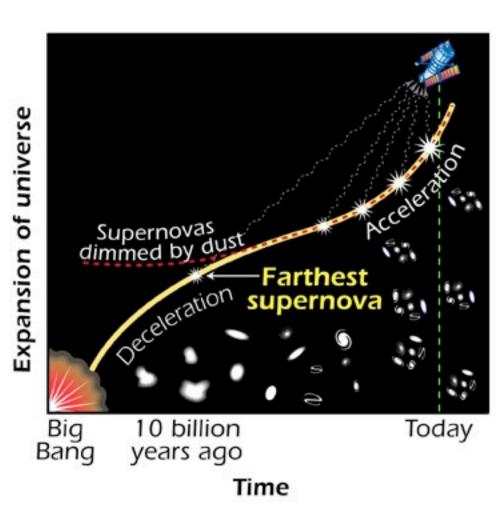
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Supernova Cosmology: Results

- Supernovae show * cosmic expansion slower in the past!?!?
- the expansion rate is speeding up with time!
- the universe is accelerating!



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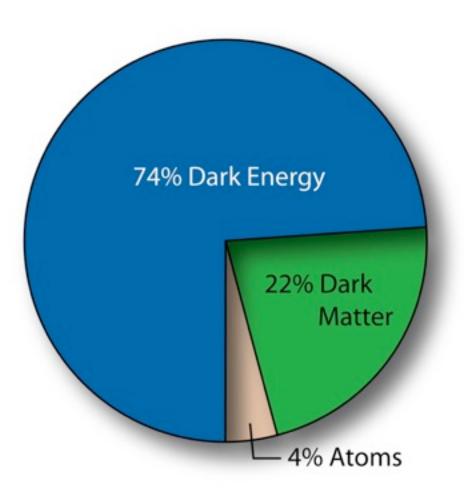
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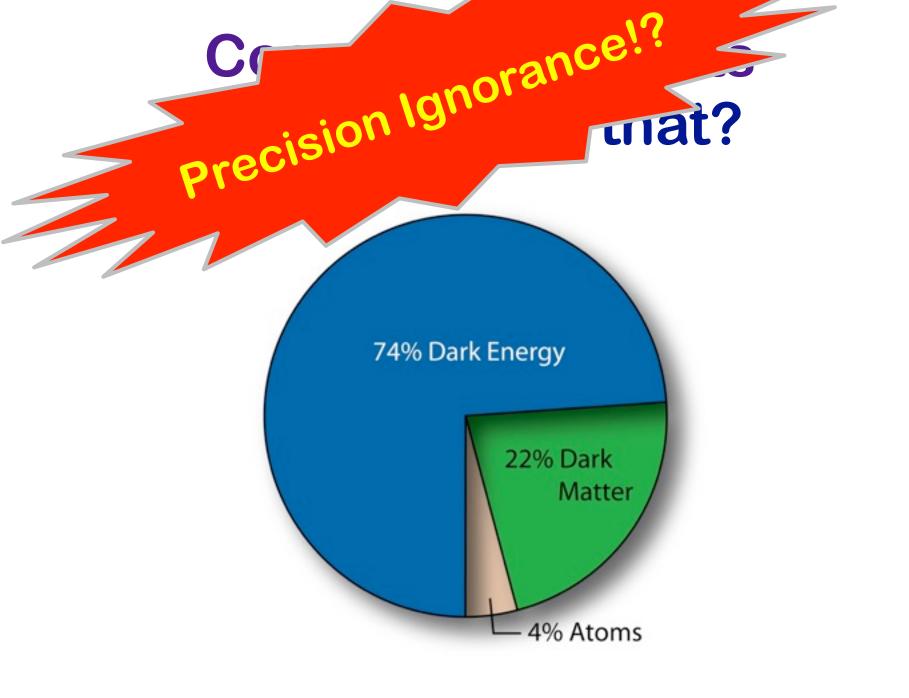
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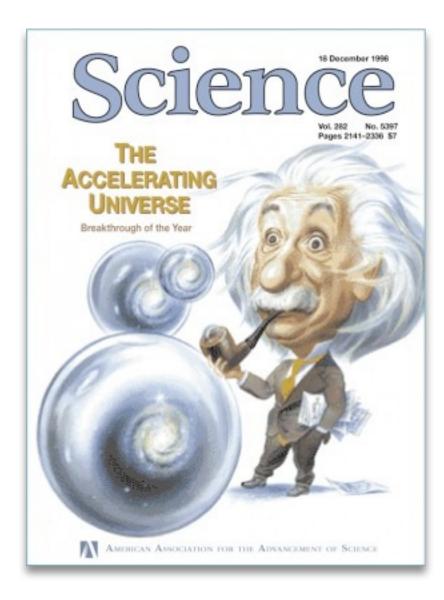
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Cosmic Ingredients Who ordered that?







Science Magazine "Breakthrough of the year"

2011 Nobel Prize in Physics



"for the discovery of the accelerating expansion of the Universe through observations of distant supernovae"



Saul Permutter



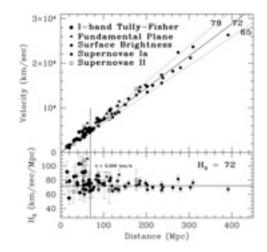
Brian Schmidt



Adam Riess

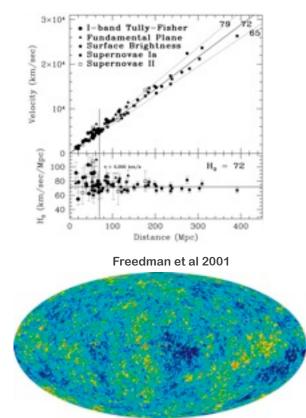
- Gravity = General Relativity Space: Homogeneous & Isotropic
- Expanding Universe t~14 Gyr; T~10⁻⁴ eV
- Cosmic Microwave Background (CMB) t~400,000 yr; T~1 eV atomic physics
- Big-Bang Nucleosynthesis (BBN) t~1 sec, T~1 MeV nuclear physics
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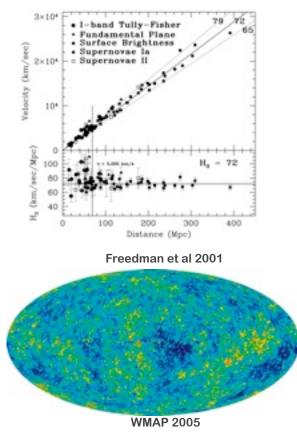


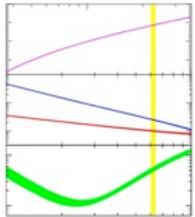
Freedman et al 2001

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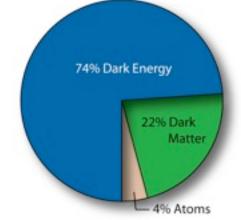


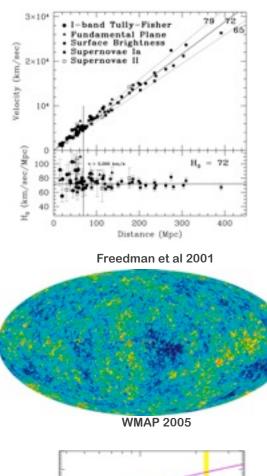


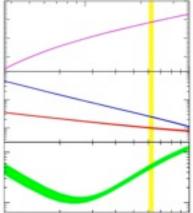


Friedmann-Lemaitre-Robertson-Walker

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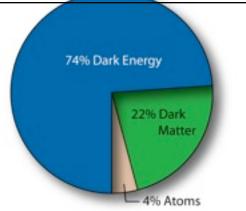


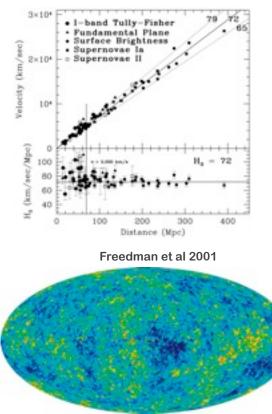




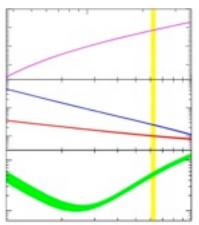
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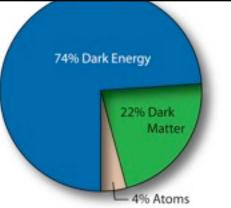


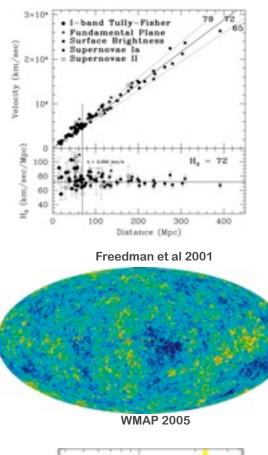


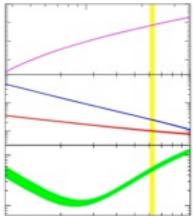


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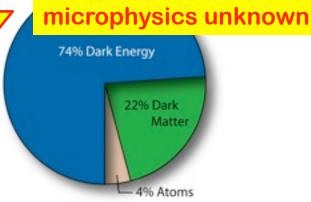


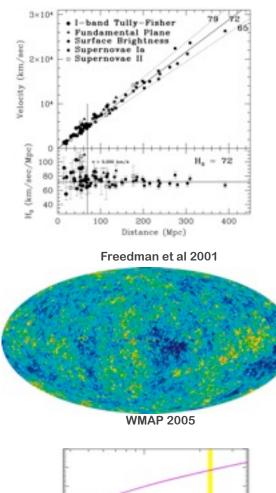
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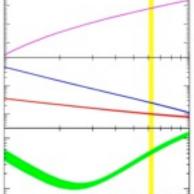
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Cosmic Job Security: Precision Ignorance

What is the dark matter?

how is it produced?

how does it interact?

what was its role in the early universe?

What is the dark energy?

 is it related to dark matter?
 does it evolve with time?
 what was its role in the early universe?

• What sets $\rho_{\text{baryon}} \sim \rho_{\text{matter}} \sim \rho_{\Lambda}$ today? compare: nuclear physics sets $\rho_{\text{H}} \sim \rho_{\text{He}}$

Questions?

Expansion and Redshifts: II

slower-n-cleaner: non-relativistic Doppler non-rel Doppler sez:

$$\frac{\delta\lambda}{\lambda} \equiv z = \frac{v}{c}$$

Hubble sez:

cz = Hr

Together

$$\frac{\delta\lambda}{\lambda} = \frac{Hr}{c}$$

But light travels distance r in time $\delta t = r/c$, so

$$\frac{\delta\lambda}{\lambda} = H\delta t = \frac{\dot{a}\delta t}{a} = \frac{\delta a}{a}$$

for arriving light, fractional λ change = fractional a change!

Worked Example: A Matter-Only Universe

consider a universe containing *only* non-relativistic matter Friedmann:

$$\left(\frac{\dot{a}}{a}\right)^{2} = \frac{8\pi G}{3}\rho - \frac{\kappa c^{2}}{R^{2}}\frac{1}{a^{2}}$$
$$= \frac{8\pi G}{3}\rho_{0}a^{-3} - \frac{\kappa c^{2}}{R^{2}}a^{-2}$$

For $\kappa = 0$: "Einstein-de Sitter"

$$(\dot{a}/a)^2 = \frac{8\pi G}{3}\rho_0 a^{-3}$$

evaluate today: $H_0^2 = 8\pi G\rho_0/3$

$$a^{1/2}da = H_0 dt$$

2/3 $a^{3/2} = H_0 t$

Q: implicit assumptions in solution?

Einstein-de Sitter:

$$t = \frac{2}{3}a^{3/2}H_0^{-1}$$
$$a = \left(\frac{3}{2}H_0t\right)^{2/3} = \left(\frac{t}{t_0}\right)^{2/3}$$

Now unpack the physics:

- boundary condition: a = 0 at $t = 0 \rightarrow$ "big bang"
- $a \propto t^{2/3}$ Q: interpretation?

• evaluate Hubble parameter

$$H = \frac{\dot{a}}{a} = \frac{21}{3t}$$

Q: interpretation?

• present age:

$$t_0 = \frac{2}{3} H_0^{-1} = \frac{2}{3} t_{\rm H}$$

Hubble time t_{H} sets scale Q: note that $t_{0} < t_{H}$: why?

- U. half its present age at $a = 2^{-2/3} = 0.63$
- objects half present separation (and 8× more compressed) at $t = 2^{-3/2}t_0 = 0.35t_0$
- using measured value of H_0 , calculate $t_0 = 8.9$ Gyr but know globular clusters have ages $t_{gc} \gtrsim 12$ Gyr Q: huh?

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• violates theorem: you can't be older than your mother!

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A: Einstein--de Sitter model is not the correct description of our Universe!

- EdS assumes matter only, and no curvature
- turns out: no curvature is correct assumption
- ...but there is stuff other than matter (and radiation!) out there!